

Fill in the blanks, and answer in the spaces provided. Show your work.

**1. Single-winner voting rules.** Suppose that there are three candidates in an election, named A, B, C, and D. There are 100 voters in total, who vote as follows:

5:  $A > B > C > D$       30:  $B > A > C > D$       10:  $D > B > A > C$   
 20:  $C > B > A > D$       35:  $D > C > B > A$

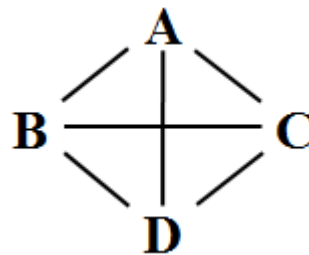
a) **Plurality.** The plurality winner is \_\_\_\_\_.

b) **Hare.** The Hare winner is \_\_\_\_\_. Use the table below to show the vote tallies in each round.

	A	B	C	D
round 1				
round 2				
round 3				

c) **Pairwise comparisons.** Construct the pairwise matrix below-left to find the candidates' scores, and construct a tournament diagram below-right, by drawing arrows from winning candidates to defeated candidates.

	A	B	C	D
A				
B				
C				
D				



d) **Borda count.** The Borda winner is \_\_\_\_\_. Show your work above.

e) **Condorcet winner, majority rule cycle.** Is there a Condorcet winner in this election? If so, who is it? Is there a majority rule cycle in this election?

**2. Rawlsian redistribution.** You are behind a Rawlsian ‘veil of ignorance’. Like everyone else, you have a  $\pi_R$  chance of being rich, in which case you will start off with a wealth of  $w_R$ , and pay a tax of  $x$ . You have a  $\pi_P$  chance of being poor, in which case you will start off with a wealth of  $w_P < w_R$ , and receive an equal share of the tax revenue from the rich, along with all of the other poor people. Redistribution is ‘leaky’, such that only a fractional portion  $\delta$  of the wealth extracted from the rich can reach the poor, while the remainder is wasted. Let  $c_P$  be your consumption if poor (after receiving your share of the tax revenue), and let  $c_R$  be your consumption if rich (after paying the tax). Let  $V(c)$  be your von Neumann-Morganstern utility function.

**a)** Suppose that  $V(c) = \sqrt{c}$ , and  $\delta = 3/5$ . Given the level of redistribution that maximizes your expected utility, what is the ratio of  $c_R$  to  $c_P$ ? (You can either bring up the first order condition from memory or derive it on the back of page 3 for bonus points.)

**b)** Suppose that  $V(c) = \sqrt{c}$ ,  $\delta = 3/5$ ,  $\pi_P = 3/4$ ,  $\pi_R = 1/4$ ,  $w_P = 80$ , and  $w_R = 1000$ . Find the value of  $x$  that maximizes your expected utility, and the resulting values of  $c_P$  and  $c_R$ .

**c)** Suppose that  $V(c) = \sqrt{c}$ , and  $\delta = 4/5$ . Given the level of redistribution that maximizes your expected utility, what is the ratio of  $c_R$  to  $c_P$ ? Do we have more redistribution or less redistribution in this case than in part a? Explain the intuition behind this as clearly as possible.

**d)** In this model, the parameter  $\delta$  is intended to convey some information about the relative inefficiency of redistributive taxation. Of course, the ‘leaky bucket’ idea is just a simplifying metaphor. Clearly explain a few reasons why redistributive taxation of income, wealth, capital, commodities, etc. create deadweight loss in the real world.

**3. Fiscal federalism.** Use your understanding of the Tiebout model and its limiting assumptions to discuss in general terms which fiscal (taxing and spending) decisions tend to be better-handled by smaller jurisdictions, and which fiscal decisions tend to be better-handled by larger jurisdictions.

**4. Proportional representation.** How does proportional representation work, and how does it differ from the plurality system that we use for most elections in the US? Create a simple numerical example in which they would give different results.